



Introduction to Wireless Networks: protocols and performance analysis

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Cumulative credits: some figures have been taken from slides found on the web, by the following authors
(in alphabetical order):

J.J. Garcia Luna Aceves (ucsc), James F. Kurose & Keith W. Ross, Jochen Schiller (fub), Nitin Vaidya (uiuc)

PHY modelling issues

- **Usually the PHY layer is considered a Black box in the simulation model (e.g. when studying higher layers)**
- **Many PHY parameters can have a deep effect on higher layers' behavior (and are inherently “continuous” ...)**
 - a modeler needs to know what is required to be modeled for obtaining significant results (e.g. mapping to “discrete”...)
 - simplifying assumptions can lead to wrong results
 - Warning: more analysis?
- **Usually the choice is to model only few parameters of the PHY layer, describing the aggregate effect of main parameters (see later) and their values' distributions.**
 - Trace driven simulation? Regression data from logged trace results?
 - e.g. channel states → Bit error rate → prob. of packet error?
 - e.g. network topology → interference → bit error rate?
 - e.g. coding and transmission technique → data rate?

PHY modelling issues

- **Homework: analytical analysis of a PHY system**

- a given channel is DSSS with 8 chips/bit
- maximum chipping rate = 2.000.000 chip/sec
- can recover up to 2 chip errors/bit
- probability of chip error = P_{ce}
- probability of a bit error?
- frame length (constant) = 1500 Bytes
- probability of frame error?

will be used as the PHY (black box) reliability parameter...

- timeout delay before packet retransmission attempt = 1 sec
- average delay before tagged frame's successful transmission?

PHY modelling issues

- **Homework: Solution**

- Probability of a bit error?

$$P_{bit_ok} = (1 - p_{ce})^8 + 8 \cdot p_{ce} \cdot (1 - p_{ce})^7 + \binom{8}{2} \cdot p_{ce}^2 \cdot (1 - p_{ce})^6$$

$$P_{bit_error} = 1 - P_{bit_ok}$$

- Probability of frame error?

1 Frame = 1500 Byte = 1500*8 bit = 1500*8*8 chip

$$P_{FrameError} = P\{at_least_one_bit_error\} = 1 - p\{all_bits_ok\}$$

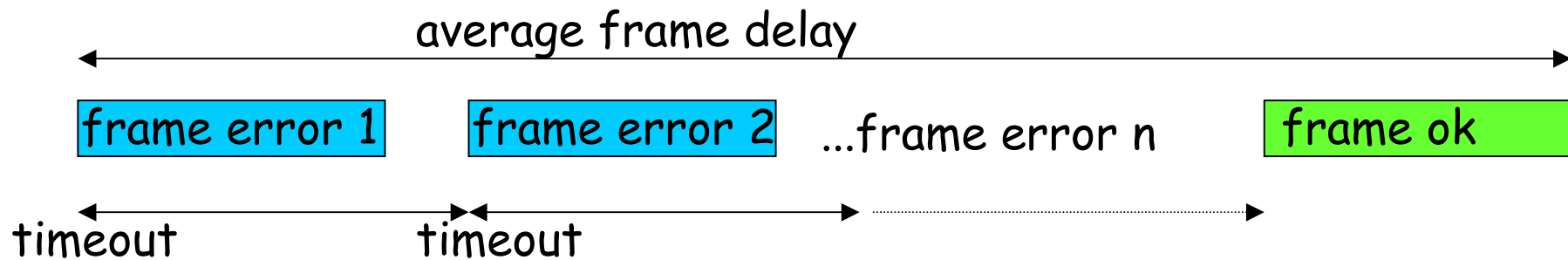
$$P_{FrameError} = 1 - P_{bit_ok}^{(1500 \cdot 8)}$$

PHY modelling issues

Homework: Solution

- Average delay before successful transmission of a tagged frame?

$$\text{Avg. Delay} = (\text{Avg.}_\text{Number_Retrans.} \cdot \text{Timeout}) + \text{Frame Delay}$$



$$\text{avg_delay} = \left[\sum_{i=1}^{\infty} i \cdot (p_{\text{FrameError}})^{i-1} \cdot (1 - p_{\text{FrameError}}) \right] \cdot \text{Timeout} + \frac{[1500 \cdot 8 \cdot 8]}{2.000.000}$$

$$\text{avg_delay} = \frac{1}{1 - p_{\text{FrameError}}} \cdot \text{Timeout} + 0.048 = \frac{1}{p_{\text{bit_ok}}^{1500 \cdot 8}} \cdot \text{Timeout} + 0.048$$

Modelling network topology and mobility

- **Fixed (static) topology**
 - fixed (static) model
- **Ad Hoc topologies**
 - many hosts with topology parameters
 - 2D position (X,Y) or 3D position (X,Y,Z)
 - Links: related to mutual reachability (mono,bi-directional)
 - TX Power (Coverage area)
 - » circular (multiple coverage sub-areas)
 - » exagonal (approximation for regular infrastructure models, e.g. cellular AP)
 - » square (highly approximated)
 - Rx sensitivity (reception threshold)
 - » Interference model?
 - » asymmetric coverage area
 - Obstacles?

Modelling network topology and mobility

■ Ad Hoc mobility

- mobility dynamically affects network topology
- many hosts with mobility parameters
 - (assume 2D position (X,Y) for simplicity)
 - host state: fixed or mobile
 - two-state model: probability distribution
 - fixed-position state : zero mobility
 - mobile state : non-zero mobility
 - » various mobility models define the mobility parameters
 - » Velocity is a vector (speed, direction, orientation)
 - » position shift is vector (Velocity*time)
- Problem: mobility is a continuous process
 - how to model mobility effects in discrete event simulation?
 - discrete quantization? -> approximation of effects
 - fine quantization -> many events -> slow simulation

Modelling network topology and mobility

- **Random Waypoint model**

- is completely random (pattern-less)
- This model is less affected by the initial position of hosts
- Host N
 - step $i = 1..I$ starting at time T_{n_i}
 - » Host N selects random target position (x,y) in the plane
 - » host N moves with constant velocity V_{n_i} (randomly generated)
 - » Step duration is a function of distance and velocity
 - node mobility is not correlated -> link failures are independent.

Modelling network topology and mobility

- **Random Direction model**

- is completely random (pattern-less)
- host mobility characterized by a sequence of "epoch"
- Host N
 - epoch $i = 1..I$ starting at time T_{n_i} with duration DT_{n_i}
 - » epoch duration DT_{n_i} is a stochastic variable, exponentially distributed, average $1/\lambda_n$ (consecutive duration independent)
 - » host N moves with constant velocity V_{n_i}
 - » host N moves in constant direction D_{n_i} (in polar coordinates)
 - » Number of epochs in a time interval t is a discrete stochastic process $N_n(t)$
 - for each host n , and for each epoch i , DT_n , V_n , D_n are NOT correlated -> node mobility is not correlated -> link failures are independent.

Modelling network topology and mobility

▪ Random Direction model

• implementation 1:

- given $\text{pos}(n,i)$ the position of node n in epoch i , and $R_n(i)$ the vector defining the movement in epoch i for node n (constant speed and direction for the time $DT_{n,i}$)

$$\text{pos}(n,i+1) = \text{pos}(n,i) + R_n(i) \cdot DT_{n,i}$$

• Implementation 2:

- $DT_{n,i}$ is constant (epoch duration is constant)
- randomly generated $\text{pos}(n,0), \text{pos}(n,1) \dots \text{pos}(n,I)$
 - » $R_n(i)$ is derived from $\text{pos}(n,i)$

• Variation:

- a node after each movement wait for a constant time

Modelling network topology and mobility

▪ Random Direction model

- how to evaluate the presence of a link between node a and b in a time interval $[t_0, t_1]$?
 - evaluate mobility of node a in $[t_0, t_1]$
 - evaluate mobility of node b in $[t_0, t_1]$
 - evaluate relative mobility of nodes a,b in $[t_0, t_1]$
 - compare with the model assumption about Tx range, etc.
 - N.B. given the model assumption, and given the model parameters, Prob (link from a to b) can be defined analitically
 - N.B. since the model assumptions make the node mobility not correlated, a route between multiple nodes (multi-hop) can be defined analitically with the joint probabilities $P(a \text{ to } b) * P(b \text{ to } c) \dots$
- This is interesting property: can validate simulation results?

Modelling network topology and mobility

- **Random Direction model**

- is the discrete counterpart of the Brownian motion
 - e.g. see http://www.phys.virginia.edu/classes/109N/more_stuff/Applets/brownian/applet.html
 - e.g. see [Project MFR](#) (credits Quadalti, Massera, Capece)
- it is not much realistic for network scenarios
- can be used sometimes as "worst case" analysis because it describes the most "unpredictable" mobility pattern
- it can be described and validated analitically

Modelling network topology and mobility

▪ Reference Point Group Mobility (RPGM)

- it relates to group mobility in ad hoc networks
- each "group" of hosts has a "logic centre"
- the "logic centre" mobility defines the global mobility parameters of the group
- mobile hosts are uniformly distributed inside the "domain area" of the "logic center" of the group
- each host has a random mobility around a "reference point" (RP) which moves relative to the "logic center" mobility

Modelling network topology and mobility

- **Reference Point Group Mobility (RPGM)**
 - implementation is based on
 - V_{gi} : vector for group motion (logic center)
 - V_{hi} : vector for host motion around RP
 - check points define discrete time advance Δt
 - at check point time t the group moves to current position
 - **Advantage**
 - can be used to model realistic scenarios
 - can be used for modelling "logged traces" of real mobility pattern (snapshot recorded as vectors V_{gi} , V_{hi} for each checkpoint)

Modelling network topology and mobility

- **Natural Random Model (NRM)**

- a model for highly predictable paths
 - assumes low variation of mobility vector vs. time
- for a given host h :
 - mobility vector $M(xv,yv)$ = the sum of
 - Base Vector $Bh(bx,by)$
 - » main (group) mobility component
 - Variance Vector $Vh(vx,vy)$
 - » models the variation from the base vector of a single host
 - maybe $MIN(xv,yv) < M(xv,yv) < MAX(xv,yv)$ to model realistic range of variation for node speed
 - by using polar coordinates, MIN and MAX variation of direction can be defined
 - finally, acceleration/deceleration can be controlled

Modelling network topology and mobility

- **Exponentially correlated random mobility (ECRM)**

- host partitioned in G groups: S_i hosts in group i

$$b(t+1) = b(t) \cdot e^{-\frac{1}{\tau}} + s \cdot \sigma \cdot \sqrt{1 - e^{-\frac{1}{\tau}}} \cdot r$$

- $b(t)$ is the position (polar coordinates) at time t
- τ is a time constant (position-change rate)
- σ is the variance for the position-changes
- s is the host speed
- r is a gaussian variable

Modelling network topology and mobility

- **Exponentially correlated random mobility (ECRM)**
 - motion of each group is independent
 - from other groups' motion
 - from motion of hosts in the group

Modelling network topology and mobility

- **Restricted random waypoint**
 - based on random waypoint
 - applied to large ad hoc networks
 - towns, highways...
 - Ordinary hosts
 - follow random waypoint modelling of towns
 - towns are geographic areas (grid)
 - commuter hosts
 - after a single motion in town, they move to another town, becoming Ordinary hosts
 - they run (constant speed and direction) over highways

Modelling network topology and mobility

- **Column model**

- model characterized by “leader” host and a set of related hosts following the leader
- each host i has a reference point $RP_i(x,y)$
- each host i has a random motion component vector RV_i with respect to its reference point RP_i
- each reference point RP has a global motion component vector AV
- position of node i at time $t+Dt$:
 - $pos(t+Dt) = RP(t+Dt) + RV(t)$
 - where $RP(t+Dt) = RP(t) + AV(t)$

Modelling network topology and mobility

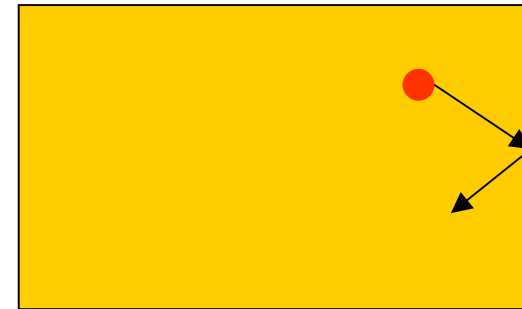
■ Pursue Model

- model similar to set of nodes following a target host
- non-target hosts are limited in the amount of distance they run towards the target in a given time by $A(\text{target_pos}(t))$ (their pursue of the target is approximated)
- non-target hosts motions are biased by the random component vector RV
- position of host i at time $t+Dt$:
$$\text{pos}(t+Dt) = \text{pos}(t) + A(\text{target_pos}(t)) + RV(t)$$

Modelling network topology and mobility

- **The area boundary policy**

- reflection (concentrate host distribution in the middle of the area)



- toroidal (uniform distribution)

