

# Retractable Contracts And Beyond



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# Map of the talk

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- Why retractable contracts?
- What is a retractable contract?
- What is a speculative contract?
- What is beyond?



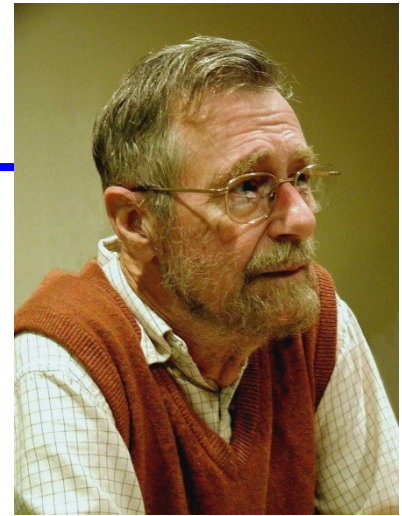
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# Undoing things considered harmful

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- Undo operations are useful and widespread
  - Undo command in your favorite editor
  - Back button in your favorite browser
  - Restore a past backup
- In interactions (unilateral) undo may lead to unpredictable or undesired results
  - What happens if you press the back button of the browser while reserving a flight?
  - You don't want a client to be able to undo her payment after a purchase
- Undo activities must be disciplined

# Contracts

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- A (binary) **contract** is the abstract description of the behaviour of a client or a server
- A client **complies** with a server if all her requirements are fulfilled
  - by reaching a distinguished satisfaction state or
  - by running an infinite interaction without ever getting stuck
- A client that does not comply with its server may get stuck

# Retractable contracts

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- We start from binary contracts
- Getting stuck may depend on wrong choices taken during the interaction
- Going back to past choices and trying different paths may solve the problem
- This will “facilitate” compliance
- We explore a notion of contracts where past decisions are stored and can be undone



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# Retractable contracts: syntax

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- $\sigma, \rho ::= 1$  success
  - $\sum_{i \in I} a_i . \sigma_i$  external input choice
  - $\oplus_{i \in I} \bar{a}_i . \sigma_i$  internal output choice
  - $\sum_{i \in I} \bar{a}_i . \sigma_i$  retractable output choice
  - $\oplus_{i \in I} a_i . \sigma_i$  internal input choice
  - $x$  variable
  - $rec\ x . \sigma$  recursion
- 
- We add  $\circ$  (no more alternatives) to contracts  $\sigma$
  - Histories are stacks of contracts  $h ::= [] \mid h : \sigma$
  - Contracts with history:  $h < \sigma$



# Motivating problem

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- A buyer wants to buy either a bag or a belt
- She will decide whether to pay by card or cash after knowing the price

$$\text{Buyer} = \overline{\text{bag}} . \text{price} . (\overline{\text{card}} \oplus \overline{\text{cash}}) \oplus \overline{\text{belt}} . \text{price} . (\overline{\text{card}} \oplus \overline{\text{cash}})$$

- The seller accepts cards only for bags, not for belts

$$\text{Seller} = \text{bag} . \overline{\text{price}} . (\text{card} + \text{cash}) + \text{belt} . \overline{\text{price}} . \text{cash}$$

- Buyer and seller are not compliant
- They become compliant if we make, e.g., the buyer choice between bag and belt retractable
- The buyer is still able to pay a belt with card if interacting with a seller allowing this

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$$\text{Seller} = \text{bag} . \overline{\text{price}} . (\text{card} + \text{cash}) + \text{belt} . \overline{\text{price}} . \text{cash}$$

- Buyer and seller are not compliant
- They become compliant if we make, e.g., the buyer choice between bag and belt retractable
- The buyer is still able to pay a belt with card if interacting with a seller allowing this

# Retractable contracts: semantics

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- Contracts are executed as usual but...
- ... branches in external choices which are not selected are stored in the history
- When the interaction is stuck, both client and server can pop from the history the last state

# Sample computation

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- Buyer =

$$[] \prec \overline{bag} . \overline{price} . (\overline{card} \oplus \overline{cash}) + \overline{belt} . \overline{price} . (\overline{card} \oplus \overline{cash})$$

- Seller =

$$[] \prec \overline{bag} . \overline{price} . (\overline{card} + \overline{cash}) + \overline{belt} . \overline{price} . \overline{cash}$$

# Sample computation

---

● Buyer =

$$[] \prec \overline{bag}.price.(\overline{card} \oplus \overline{cash}) + \overline{belt}.price.(\overline{card} \oplus \overline{cash})$$

$$\rightarrow [] : \overline{bag}.price.(\overline{card} \oplus \overline{cash}) \prec \overline{price}.(\overline{card} \oplus \overline{cash})$$

● Seller =

$$[] \prec \overline{bag}.price.(card + cash) + \overline{belt}.price.cash$$

$$\rightarrow [] : \overline{bag}.price.(card + cash) \prec \overline{price}.cash$$

# Sample computation

---

- Buyer =

$$[] \prec \overline{bag} . \overline{price} . (\overline{card} \oplus \overline{cash}) + \overline{belt} . \overline{price} . (\overline{card} \oplus \overline{cash})$$

$$\rightarrow [] : \overline{bag} . \overline{price} . (\overline{card} \oplus \overline{cash}) \prec \overline{price} . (\overline{card} \oplus \overline{cash})$$

$$\rightarrow [] : \overline{bag} . \overline{price} . (\overline{card} \oplus \overline{cash}) : \circ \prec \overline{card} \oplus \overline{cash}$$

- Seller =

$$[] \prec \overline{bag} . \overline{price} . (\overline{card} + \overline{cash}) + \overline{belt} . \overline{price} . \overline{cash}$$

$$\rightarrow [] : \overline{bag} . \overline{price} . (\overline{card} + \overline{cash}) \prec \overline{price} . \overline{cash}$$

$$\rightarrow [] : \overline{bag} . \overline{price} . (\overline{card} + \overline{cash}) : \circ \prec \overline{cash}$$



# Sample computation

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- Buyer =

$$[]: \overline{bag}.price.(\overline{card} \oplus \overline{cash}): \circ \prec \overline{card} \oplus \overline{cash}$$

- Seller =

$$[]: \overline{bag}.price.(\overline{card} + \overline{cash}): \circ \prec \overline{cash}$$

# Sample computation

---

● Buyer =

$$[]: \overline{bag}.price.(\overline{card} \oplus \overline{cash}): \circ \prec \overline{card} \oplus \overline{cash}$$

$$\rightarrow []: \overline{bag}.price.(\overline{card} \oplus \overline{cash}): \circ \prec \overline{card}$$

● Seller =

$$[]: \overline{bag}.price.(\overline{card} + \overline{cash}): \circ \prec \overline{cash}$$

# Sample computation

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- Buyer =

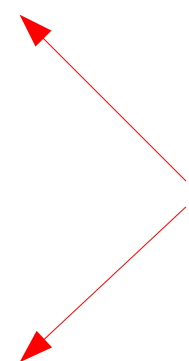
$$[]: \overline{bag}.price.(\overline{card} \oplus \overline{cash}): \circ \prec \overline{card} \oplus \overline{cash}$$

$$\rightarrow []: \overline{bag}.price.(\overline{card} \oplus \overline{cash}): \circ \prec \overline{card}$$

- Seller =

$$[]: \overline{bag}.price.(\overline{card} + \overline{cash}): \circ \prec \overline{cash}$$

Interaction  
is stuck



# Sample computation

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- Buyer =

$$[]: \overline{bag}.price.(\overline{card} \oplus \overline{cash}): \circ \prec \overline{card}$$

- Seller =

$$[]: \overline{bag}.price.(\overline{card} + \overline{cash}): \circ \prec \overline{cash}$$

# Sample computation

---

● Buyer =

$$[]:\overline{bag}.price.(\overline{card} \oplus \overline{cash}): \circ < \overline{card}$$

$$\rightarrow []:\overline{bag}.price.(\overline{card} \oplus \overline{cash}) < \circ$$

● Seller =

$$[]:\overline{bag}.\overline{price}.(card+cash): \circ < cash$$

$$\rightarrow []:\overline{bag}.\overline{price}.(card+cash) < \circ$$

# Sample computation

---

- Buyer =

$$[]: \overline{bag}.price.(\overline{card} \oplus \overline{cash}): \circ < \overline{card}$$

$$\rightarrow []: \overline{bag}.price.(\overline{card} \oplus \overline{cash}) < \circ$$

$$\rightarrow [] < \overline{bag}.price.(\overline{card} \oplus \overline{cash})$$

- Seller =

$$[]: \overline{bag}.price.(\overline{card} + \overline{cash}): \circ < \overline{cash}$$

$$\rightarrow []: \overline{bag}.price.(\overline{card} + \overline{cash}) < \circ$$

$$\rightarrow [] < \overline{bag}.price.(\overline{card} + \overline{cash})$$



# Sample computation

---

● Buyer =

$$[] \prec \overline{bag}. \overline{price}. (\overline{card} \oplus \overline{cash})$$

● Seller =

$$[] \prec \overline{bag}. \overline{price}. (card + cash)$$

# Sample computation

---

● Buyer =

$$[] \prec \overline{bag}. \overline{price}. (\overline{card} \oplus \overline{cash})$$

$$\rightarrow []:\circ \prec \overline{price}. (\overline{card} \oplus \overline{cash})$$

● Seller =

$$[] \prec \overline{bag}. \overline{price}. (card + cash)$$

$$\rightarrow []:\circ \prec \overline{price}. (card + cash)$$

# Sample computation

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- Buyer =

$$[] \prec \overline{bag}. \overline{price}. (\overline{card} \oplus \overline{cash})$$

$$\rightarrow []:\circ \prec \overline{price}. (\overline{card} \oplus \overline{cash})$$

$$\rightarrow []:\circ:\circ \prec \overline{card} \oplus \overline{cash}$$

- Seller =

$$[] \prec \overline{bag}. \overline{price}. (card + cash)$$

$$\rightarrow []:\circ \prec \overline{price}. (card + cash)$$

$$\rightarrow []:\circ:\circ \prec card + cash$$

# Sample computation

---

● Buyer =

$$[]: \circ : \circ < \overline{card} \oplus \overline{cash}$$

● Seller =

$$[]: \circ : \circ < card + cash$$

# Sample computation

---

● Buyer =

$$[]:\circ:\circ \prec \overline{card} \oplus \overline{cash}$$

$$\rightarrow []:\circ:\circ \prec \overline{card}$$

● Seller =

$$[]:\circ:\circ \prec card + cash$$

# Sample computation

---

● Buyer =

$$[]: \circ : \circ < \overline{card} \oplus \overline{cash}$$

$$\rightarrow []: \circ : \circ < \overline{card}$$

$$\rightarrow []: \circ : \circ : \circ < 1$$

● Seller =

$$[]: \circ : \circ < card + cash$$

$$[]: \circ : \circ : cash < 1$$



# Compliance

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- We can use the standard notion of compliance
  - If the computation gets stuck, then the client is satisfied
- We can define a formal system to decide compliance
- The main novelty is that two external choices are compliant iff there exists a compatible branch

$$\Gamma, \alpha.\rho + \rho' \dashv \bar{\alpha}.\sigma + \sigma' \triangleright \rho \dashv \sigma$$

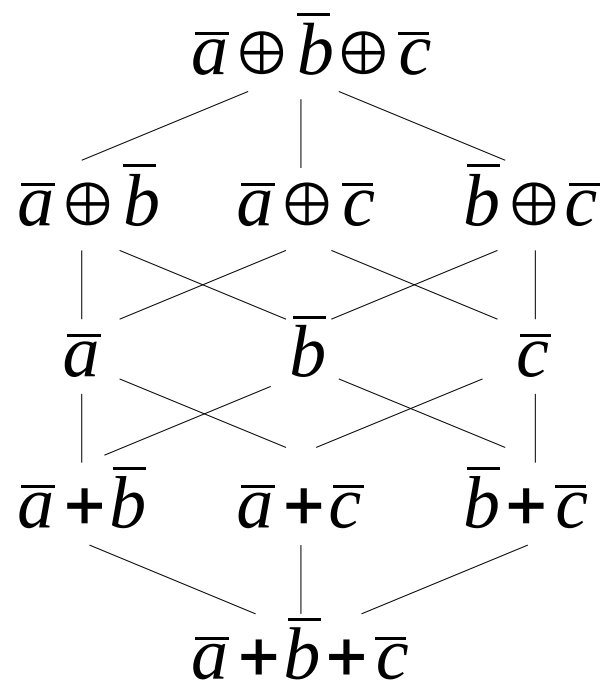
$$\frac{}{\Gamma \triangleright \alpha.\rho + \rho' \dashv \bar{\alpha}.\sigma + \sigma'}$$

- The formal system is correct, complete and terminating, hence it can be transformed into a procedure
- The procedure requires  $O(n^5)$ 
  - More than for standard contracts

# Duality and subcontract relation

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- From the notion of compliance we can define a notion of subcontract
  - Replacing a contract with a subcontract preserves compliance
- The syntactic dual is also a semantic dual
  - The more general compliant contract



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# Speculative contracts

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- We start again from binary contracts
- For efficiency reasons one may want to try different options concurrently
- As soon as one of them succeeds, the whole computation is successful
- We use the same syntax that we used for retractable contracts
  - Now external choice among outputs has the speculative behaviour above
  - External since the environment can slow down undesired paths selecting the one he wants to succeed

# Speculative contracts: results

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- The decision procedure for retractable contracts and for speculative contracts coincide
- As a consequence, all the results about compliance, duality and subcontract apply

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# Summary

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- We presented a model of contracts with retractable choice
  - Compliance
  - Subcontract relation
  - Duality
- Simple and neat extension of the theory of binary contracts
- Using retractable choice instead of normal choice extends the set of compliant contracts
- The same theory captures also speculative execution

# What is beyond?

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- Explore the notion of retractable contracts in multiparty sessions
- Are there other meaningful ways to exploit contracts/behavioural types to control reversibility?
- Are there other useful computational patterns that can be tamed using contracts?





End of talk

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Thanks!

Questions?

# Most related work

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Franco Barbanera, Mariangiola Dezani-Ciancaglini, Ugo de'Liguoro: Compliance for reversible client/server interactions. BEAT 2014

also considered contracts with rollback

BEAT 2014	vs	PLACES 2015
● Free rollback	vs	rollback only when stuck
● Explicit checkpoint	vs	implicit checkpoint
● One checkpoint	vs	stack of checkpoints
● <b>Compliance harder</b>	<b>vs</b>	<b>compliance easier</b>